Stochastic modelling of muscle recruitment during activity

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ABSTRACT

Muscle forces can be selected from a space of muscle recruitment strategies that produce stable motion and variable muscle and joint forces. However, current optimization methods provide only a single muscle recruitment strategy. We modelled the spectrum of muscle recruitment strategies while walking. The equilibrium equations at the joints, muscle constraints, static optimization solutions, and 15-channel electromyography recordings for seven walking cycles were taken from earlier studies. The spectrum of muscle forces was calculated using Bayesian statistics and MCMC while EMG-driven muscle forces were calculated using EMG-driven modelling. We calculated the differences between the spectrum and EMG-driven muscle force for 1 to 15 input EMGs and we identified the muscle strategy that best matched the recorded electromyography pattern. The best-fit strategy, static optimization solution, and EMG-driven force data were compared using correlation analysis. Possible and plausible muscle forces were defined as within physiological boundaries and within EMG boundaries. Possible muscle and joint forces were calculated by constraining the muscle forces between zero and the peak muscle force. Plausible muscle forces were constrained within six selected EMG boundaries. The spectrum to EMG-driven force difference increased from 40 N to 108 N for 1 to 15 EMG inputs. The best-fit muscle strategy better described the EMG-driven pattern (R^2 = 0.94; RMSE = 19 N) than the static optimization solution (R^2 = 0.38; RMSE = 61 N). Possible forces for 27 of 34 muscles varied between zero and the peak muscle force, inducing a peak hip force of 11.3 body-weights. Plausible muscle forces closely matched the selected EMG patterns; no effect of the EMG constraint was observed on the remaining muscle force ranges. The model can be used to study alternative muscle recruitment strategies in both physiological and pathophysiological neuromotor conditions.

KEYWORDS

Subject-specific musculoskeletal models; Bayesian muscle force simulator; statistical muscle recruitment; personalized lower-limb loads; level walking; human locomotion; muscle synergy; muscle load sharing; muscle recruitment.

INTRODUCTION

Internal forces that physical activity engender on our skeleton through muscles and joints are important for studying human motion [1] and skeletal mechanics [2]. However, the biomechanical assessment of muscle forces is difficult because the musculoskeletal system is highly redundant [3] and the sensorimotor control system is intrinsically variable [4]. Muscles recruitment targets multiple and competing goals, and depends on the task being executed, subjective healthy condition and noise that plague the sensory inputs and muscles output in determining the appropriate motor command [5]. A better understanding of the repertoire of alternative sensorimotor control strategies may reveal important in studying human motion and skeletal mechanics [5].

According to the uncontrolled manifold hypothesis, our central nervous system uses all the redundant degrees of freedom to ensure flexible and stable motion [6]. Possible muscle synergies can therefore be defined as organizations of muscle forces that stabilize joint torques and motion; or, in other words, alternative solutions to the muscle load sharing problem. Körding and Wolpert showed that our central nervous system (CNS) likely interprets the problem of optimal performance in a statistical fashion by weighting knowledge gathered from previous experiences and information gathered from multiple sensory modalities [4]. By considering both types of information in the form of prior and likelihood, Bayesian statistics have been shown to properly describe the mechanism behind the generation of movement trajectories [7], forces [8] and judgment timing [9]. Likewise, our CNS may solve the muscle load sharing problem [4] by recruiting muscles from a space of alternative solutions, ensuring stable motion [6]. However, the large majority of current methods used for calculating muscle forces target, among the infinite possible solutions, the single muscle synergy that minimizes a chosen cost function [10].

By using different energy- and stress-based cost functions, static optimization methods have been shown to provide muscle force patterns that are in qualitative agreement with the recorded electromyography (EMG) [11]. However, static optimization methods are known to underestimate the contribution of balanced agonist-antagonist muscle contractions [12], the so-called muscle co-contractions, which are essential in a number of circumstances. For example, muscle co-contractions are important in (a) controlling the joint impedance and stability during daily activities [13] and (b) for executing motions characterized by rapid changes of joint torque, such as those occurring while landing [14] and running [15]. Muscle co-contractions have also been found to determine the hip force during activity in terms of magnitude, distribution and timing [13,16]. In cats, the static optimizations solution has been shown a poor predictor of the soleus and gastrocnemius force pattern [17].

EMG-driven methods have been developed to calculate muscle force patterns that follow the muscle electrical activity recorded using electromyography (EMG). EMG-driven muscle forces are calculated by inputting the EMG signal to muscle excitation- and contraction-dynamic models, which are then used to solve the dynamic problem of the motion [18–20]. However, model simplifications and measurement errors cause inconsistencies between the motion being studied and the calculated EMG-driven muscle forces. Inverse EMG-driven models solve the muscle load sharing problem by forcing the static optimization solution within an arbitrarily defined interval around the calculated EMG-driven muscle force to ensure that a solution to the problem exists [19]. Forward EMG-driven models use optimization-based procedures to tune the model so that the calculated EMG-driven muscle forces generate the desired motion of the model [18,20]. Lloyd and Besier [18] used an EMG-driven model of the knee-spanning muscles to estimate the knee torque. Sartori et al. [20] used a lower-limb model to calculate muscle forces during walking, running, sidestepping and crossover cutting manoeuvres. However, the single representative muscle synergy calculated using both EMG-driven and static optimization

79 methods cannot provide information about the spectrum of muscle synergies driving motion
80 [18–20].

81 Another possibility is to explore the entire solution space of the muscle load-sharing problem
82 [21]. The space of physiologically possible muscle synergies can be described as the solution
83 space of the inverse, highly indeterminate, linear problem of muscle equilibrium at the joints,
84 which can be geometrically represented by a bounded portion of a hyper-plane in the muscle
85 force domain [11]; its orientation, offset and boundaries are respectively determined by the
86 muscle lever arms, joint torques and physiological constraints of muscle force. Heino *et al*. [22]
87 combined Bayesian statistics and Markov Chain Monte Carlo (MCMC) methods for exploring
88 the solution space of highly indeterminate inverse linear problems in a software called
89 METABOLICA, which uses Bayesian statistics to estimate the posterior probability density
90 function (PDF) for the unknowns and the MCMC algorithm to sample the estimated PDF. By
91 constraining muscle forces between zero and the muscle peak force, this approach has been
92 used to explore the muscle potential to generate force during a single walking frame [21]. No
93 study has investigated the natural unpredictable variability of muscle forces during activity.
94 Combining musculoskeletal models, Bayesian statistics, MCMC sampling methods and EMG-
95 driven muscle force modelling is a viable solution for calculating the spectrum of either
96 potential or physiologically plausible musculoskeletal forces during activity.

97 The aim of this study was to investigate the repertoire of muscle synergies during walking.
98 The lower-limb joint torques, muscle lever arms, muscle force constraints and the EMG signals
99 for seven walking trials were taken from earlier studies [23,24]. The spectrum of muscle
100 recruitment strategies was calculated using Bayesian statistics and MCMC sampling methods,
101 while EMG-driven muscle forces were calculated using the available EMGs and a Hill-type
102 muscle excitation- and contraction-model. The model was characterised by studying the
103 consistency between EMG-driven forces and the model of the motion, and comparing the

proposed method with a commonly used static optimization procedure. Finally, the muscle potential to generate force and the spectrum of physiologically plausible muscle forces were calculated and analysed.

MATERIALS AND METHODS

Model development

The model, developed for studying possible muscle recruitment strategies during motion, was based on an earlier lower-limb model of a complete stride [23]. The complete motion capture is available for download at www.physiomespace.com (key-word: LHDL_1stMatchedVolunteer_MOCAP). EMGs were recorded for 15 lower-limb muscles (i.e., gluteus maximus, gluteus medius, rectus femoris, vastus lateralis, vastus medialis, semitendinosus, biceps femoris long head, tibialis anterior, extensor digitorum, extensor hallucis, peroneus longus, soleus, gastrocnemius lateralis, gastrocnemius medialis, flexor digitorum) using a TelEMG® system (BTS, Milan, Italy, 2000 Hz). The model, implemented in Matlab (The MathWorks, Natick, MA, USA), is generic in that it can be used to study the muscle load sharing problem of any musculoskeletal model and task of motion. The analysis is described in four parts: (1) the gait model; (2) the calculation of the muscle force potential, hereinafter referred to as physiologically possible muscle forces; (3) the calculation of the spectrum of muscle forces that represent the unpredictable variability of the muscle recruitment process, hereinafter referred to as physiologically plausible muscle forces; and, (4) data analysis.

The gait model

The musculoskeletal model, including the joint angles and torques while walking was obtained from earlier studies [23,25,26] (Fig. 1). In summary, the lower-limb musculoskeletal model was a muscle-actuated articulated system based on the work of Delp et al. [27], whose anatomy was taken from the computed-tomography images and dissection of an 81 year-old female donor (63 kg weight, 167 cm height). The articulated system was a 13-segment, 15 degree-of-freedom system, actuated by 84 Hill-type muscle-tendon units. The inertial

properties were calculated assuming homogenous bone (1.42 g/cm^3) and soft-tissue (1.03 g/cm^3) density [28]. The physiological cross section area (PCSA) was calculated from the muscle volume and length. The peak isometric muscle stress was assumed equal to 1.37 MPa, the upper bound of published values [29]. The remaining muscle parameters were based on the work of Delp et al. (1990). The gait simulation used skin-mounted marker trajectories (Vicon Motion Capture, Oxford UK, 100 Hz) and ground reaction forces at both feet (Kistler Instrument AG, Switzerland, 2000 Hz), recorded following the protocol proposed by Leardini et al. (2007) [30]. Joint angles and torques were calculated using the inverse kinematic, dynamic and static optimization algorithms implemented in Opensim [31]. The model yielded joint torques within published values, hip contact forces in agreement with in vivo measurements and muscle force patterns in good qualitative agreement with corresponding EMG recordings [23,25,26].

Physiologically possible muscle and joint forces

Physiologically possible muscle forces are defined as muscle forces within physiological boundaries, generating the joint torque from inverse dynamics and assuming that muscle activation can range from zero to full activation. Therefore, the muscle's force generating potential is represented by the boundaries of physiologically possible muscle forces. For each walking frame, the instantaneous equilibrium equation at the joints (Eq. 1), representing the muscle load sharing problem, was determined by extracting the muscle lever arm, the muscle constraints and the net joint torques from an earlier simulation of walking [23]. The equation takes the form

$$\begin{cases} \bar{\bar{B}} \times \bar{F} = \bar{M}; \bar{\bar{B}} \in \Re^{m \times n}; \bar{F} \in \Re^{n}; \bar{M} \in \Re^{m} \\ \bar{F_l} < \bar{F} < \bar{F_u} \end{cases} \quad \text{Eq. 1}$$

where $\bar{\bar{B}}$ is the matrix of muscle lever arms, $\bar{F}$ is the muscle force vector, $\bar{M}$ is the joint torque vector, $\bar{F_l}$ and $\bar{F_u}$ are respectively the lower and the upper muscles force boundaries, m is the

number of degree-of-freedom of the articulated system and *n* is the number of muscles in the model. The peak muscle force was calculated using a Hill-type muscle model. The active and passive force-length relationships were taken from the work of Thelen [32], while the force-velocity relationship was taken from the work of Delp et al. [27]. Muscle force vectors within the spectrum were categorised using a single parameter, or muscle co-contraction, defined as the difference between the actual muscle force and the minimal force required to generate a given joint torque. Each muscle force vector, solution of the muscle recruitment problem, was thus composed by a first minimal co-contraction component, represented by the static optimization solution, and a second component or muscle co-contraction force component. The muscle co-contraction level was assumed the fraction between the actual muscle co-contraction force component and the difference between the peak muscle force and the static optimization solution. The lower bound of muscles force $\bar{F}_l$ was set to zero, mimicking the muscle inability to sustain compressive forces. The upper bound of muscle forces $\bar{F}_u$ was defined by studying five uniformly distributed co-contraction levels from zero (i.e., the optimization solution) to full co-contraction (i.e., the peak muscle force vector). Samples of physiologically possible muscle forces, solutions of Eq. 1, were calculated using METABOLICA [22]. The software interprets the vector of muscle forces $\bar{F}$ as a multivariate random variable characterized by its probability density function (PDF) and it samples the calculated PDF using a Markov Chain Monte Carlo (MCMC) algorithm. The vector of muscle force $\bar{\mathrm{F}}$ was assumed uniformly distributed [21]. Thus, the prior probability density function of muscle forces takes the form

$$\pi_{pr}(\bar{F}) \; \alpha \; \Theta(\bar{F})\,\Theta(\bar{F}_u - \bar{F}) \qquad \text{Eq. 2}$$

where $\Theta(\bar{F})$ takes on the value of one if all components of the argument are positive and vanishes otherwise. The posterior PDF describing how $\bar{F}$ is distributed is

$$\pi(\bar{F}|\bar{M}) \; \alpha \; \pi_{pr}(\bar{F})\pi(\bar{M}|\bar{F}) \qquad \text{Eq. 3}$$

meaning that the posterior probability density function of muscle forces $\pi(\bar{F}|\bar{M})$ is proportional to the prior PDF, $\pi_{pr}(\bar{F})$, and the sensory information about the system states $\pi(\bar{M}|\bar{F})$, or likelihood. The stability of motion was defined by assuming the joint torque vector $\bar{M}$ the deterministic value calculated using inverse dynamics. For each walking frame, Markov Chain Monte Carlo (MCMC) algorithm was used to generate the ensemble $\{\bar{F}^0, \bar{F}^1, \dots, \bar{F}^n\}$ of 200,000 samples whose entries are random realizations drawn from Eq. 3. The null space of the matrix $\bar{\bar{B}}$, containing the muscle lever arm extracted from the model [23], is calculated using Singular Value Decomposition. The vector $\bar{F}$ is decomposed into a component $\bar{F_1}$ lying on the null space and a component $\overline{F_2}$ orthogonal to $\bar{F_1}$. Samples are drawn from the solution space using an MCMC algorithm by separately sampling the component $\bar{F_1}$ using a hit-and-run algorithm and the component $\overline{F_2}$ using a Gibbs algorithm [22].

The hip, knee and ankle reaction forces were calculated using the equation

$$\overline{JR} = \overline{JR}_d + \sum_{i=1}^{n} \bar{F}_i \qquad \text{Eq. 5}$$

where $\overline{JR}_d$ is the joint reaction force vector calculated using inverse dynamics, and $\bar{F}_i$ is the i^{th} joint-spanning muscle force vector.

Physiologically plausible muscle forces

Physiologically plausible muscle forces are defined as forces most likely to occur during normal gait and can be seen as a sub-group of the physiologically possible muscle forces. Therefore, physiologically plausible muscle forces were calculated by combining physiologically possible muscle forces and the variability of the muscle electrical activity from repeated EMGs.

Muscle forces were calculated using EMGs and Hill-type excitation- and contraction-dynamic models according to the guidelines proposed by Zajac [33]. The raw EMG signal was band-pass filtered (zero-pole-gain design, 8th order, Butterworth filter) with cut-off frequencies

of 10 and 400 Hz to minimize noise due to motion artifacts and the EMG amplifier [34]. The filtered EMG signal was rectified and low-pass filtered (zero-pole-gain design, 2nd order, Butterworth filter) with cut-off frequency of 6 Hz [33] and a 22 ms electromechanical delay, representing the muscle time response to stimuli, applied to synchronize the processed signal with the muscle response [35]. Normalisation of the processed EMG signal was then necessary to obtain a signal between zero and one representing muscle activation [33]. We scaled the processed EMG signal to match the peak muscle activation calculated using static optimization [23]. The EMG-driven muscle force was calculated using the calculated muscle activation, the active and passive force-length relationships from the work of Thelen [32] and the force-velocity relationship from the work of Delp et al. [27] for all seven gait repetitions. The force range, that is, the upper ($\bar{F}_u$) to the lower ($\bar{F}_l$) bound of muscle forces of physiologically plausible muscle forces, was assumed at the 0.68 quantile (i.e. mean ± SD) of the EMG-driven muscle force distribution projected onto the solution space of Eq. 1. Samples of physiologically plausible muscle forces were generated using METABOLICA by constraining muscle forces within the calculated force range for selected muscles and between zero and the peak physiological force for the remaining muscles.

Data analysis

Simulations were run on a desktop PC (Window 7, 64 bit, Intel Xenon E5-2630 v2, 2.60 GHz, 64 GB of memory). The gait cycle was divided into clusters of time frames and processed by 12 different CPUs using parallel computing. The speed in generating muscle force samples was output by the code.

The gait model was assessed by comparing the donor's PCSAs to corresponding measurements from donors of 83±9 year of age [36]. The muscle lever arm and the joint torques in the model were compared to corresponding published values [36–40]. Calculation of muscle forces were verified by comparing the joint torque generated by the muscles with that calculated

using inverse dynamics. The consistency between the EMG-driven muscle forces and the motion was assessed by using the distance between the EMG-driven muscle forces and the solution space of Eq. 1 as the metric; the average force distance over gait and muscles, and the muscle-by-muscle average distance during gait were calculated. The nearest muscle force vector to the EMG-driven force vector, henceforth referred to as the best-fit solution, was used for comparing the ability of the present method with that of a commonly used static optimization procedure in describing the recorded EMG pattern. To this purpose, we calculated (a) the linear regression between the EMG-driven muscle force and the best-fit muscle force, and (b) the linear regression between the EMG-driven muscle force and the static optimization solution obtained by minimizing the squared sum of muscle stress [27,31].

Alternative muscle recruitment strategies were studied in terms of physiologically possible and plausible muscle and joint forces. Physiologically possible forces were assessed by plotting the boundaries of muscle and joint forces for a progressive increase of the muscle co-contraction level. Physiologically plausible muscle forces were calculated by inputting to the model a sub-set of EMGs [19]; for this study we used six of the principal lower-limb muscles spanning the hip, the knee and the ankle (gluteus maximus, rectus femoris, vastus lateralis, biceps femoris long head, tibialis anterior and gastrocnemius medialis). The available EMGs not input to the model were compared with the respective force spectrum from the model.

RESULTS

The process resulted in 103 M and 20.6 M of different muscle forces respectively representing potential and plausible muscle forces driving walking. The algorithm generated 909 muscle force vectors, solution of Eq. 1, per second per processor.

The model anatomy and motion were in agreement with earlier studies. The muscle lever arms were consistent with those reported in earlier theoretical and experimental studies [37–39,41–44] (Table 1). The average donor's muscle PCSA was 6.15 cm^2, which represent the 25^{th} lower percentile of the elderly population reported by Ward et al. [36] (Table 2). The joint torques pattern was in agreement with that reported by Benedetti and co-workers [40] (Fig. 2). The highest unbalance between the joint torque driving walking and the net joint torque produced by the muscles was $3x10^{-11}$ Nm. The distance between the model and the EMG-driven force, averaged over gait and muscles, was below 40 N, while the peak muscle-by-muscle average distance over gait increased up to 108 N for 15 EMGs input to the model (Fig. 3). The best-fit solution better represented the EMG pattern than it did the static optimization solution (Fig. 4). The coefficient of determination between the best-fit solution and EMG-driven muscle forces was $R^2 = 0.94$, and the average error was RMS = 19 N (Fig. 5). The static optimization solution showed major discrepancies in the muscle force pattern during (a) the early stance phase of walking for the rectus femoris, (b) the stance-to-swing phase for the rectus femoris and the biceps femoris long head, and (c) the late swing phase for the gluteus maximus and the tibialis anterior. The coefficient of determination between the static optimization solution and EMG-driven muscle forces was $R^2 = 0.38$, and the average error was RMSE = 61 N.

Physiologically possible muscle synergies comprised muscle forces ranging from zero to the peak muscle force for most muscles. Twenty-seven out of the 34 lower-limb muscles ranged from zero to their peak force whereas seven muscles (gluteus maximus, adductor magnus, semimembranosus, vastus medialis, vastus lateralis, vastus medialis and soleus) couldn't reach

their peak force. The resulting upper and lower boundaries of the hip, knee and ankle force spectrums showed typical double-peak patterns; the upper force boundary reached 11.3 BW, 6.2 BW, 7.6 BW, and the lower boundary reached 4.4 BW, 2.5 BW and 3.5 BW at the hip, the knee and the ankle, respectively. Increasing the upper boundary of the muscle force up to 60% muscle co-contraction caused a proportional shift upward of the upper force boundary of possible muscle and joint forces. Further increasing the upper bound of muscle forces caused a complex non-linear response of muscle and joint forces. Negligible changes of the lower force boundary were observed by allowing different muscle co-contraction levels (Fig. 6 and 7). Physiologically plausible muscle forces well represented the pattern of the muscle electrical activity (Fig. 8 and 9). The gluteus maximus showed a consistent double-peak activity, reaching its peak values during the early stance (5% gait) and mid-swing (65% gait) phases of walking. The biceps femoris long head peaked at 10%, 50% and 90% gait. The rectus femoris peaked at heel strike (7% gait) and prior to toe-off (50% gait). The vastus lateralis peaked at heel-strike (5% gait) and prior to toe-off (43% gait). The medial gastrocnemius peaked at 40% gait and showed a smaller second peak at mid-swing (70% gait). The tibialis anterior showed a double-peak activity, reaching its peak at early stance (5% gait) and mid-swing (75% gait). The EMG-driven force range for the gluteus medius, vastus medialis, semitendinosus, extensor hallucis, extensor digitorum, peroneus longus, soleus, gastrocnemius lateralis and flexor digitorum, which were not input to the model, was smaller than the calculated force range (Fig. 9).

DISCUSSION

The aim of this study was to investigate possible muscle synergies during walking. We used a human gait model in conjunction with Bayesian statistics, MCMC sampling method and EMG-driven muscle force modelling to calculate muscle forces in full respect of physiological and dynamical constraints. The gait model provided reliable information about all the relevant musculoskeletal parameters during walking, including muscle lever arm, muscle size and joint

torques [36–40]. Muscle forces were calculated in an efficient manner, providing information about (a) the potential muscle and joint forces, and (b) the spectrum of muscle forces consistent with the muscle electrical activity input to the model.

The algorithm generated 909 muscle force samples per second per processor. Therefore, the present method can be used to calculate the spectrum of muscle forces during motion on standard desktop machines and can take advantage from using parallel computing on multiprocessor systems. The model could well represent, on average, EMG-driven muscle forces. However, the muscle-by-muscle distance between the model solutions and the EMG-driven muscle forces increased for an increasing number of EMG signals input into the model. This inconsistency may explain why EMG-driven models may not offer a solution when several EMGs are input to the model [19]. Other authors optimized the model parameters within physiological boundaries, solving the model consistency problem and ensuring that a solution to the motion problem exists [18,20,45]. However, the optimized model likely provides little information about how the calculated solution represents the subject under study because of the typically large variability of physiological parameters. More work is necessary to understand how model simplifications and input errors influence model calculations. To this purpose, the proposed method is well suited to take in input the variability of joint torques and EMGs, either caused by the natural unpredictable variability of motion or by uncertainties on measurements. The best-fit solution in the model more closely represented ($R^2 = 0.94$) the muscle electrical activity than a static optimization procedure ($R^2 = 0.38$) largely accepted for simulating normal walking [11,31], without requiring any assumptions about the adopted sensorimotor behaviour. Therefore, the proposed method can be used to calculate muscle forces when the objective of the sensorimotor behaviour is variable or not known, including in the instances of either physiological or pathophysiological neuromotor conditions.

Physiologically possible muscle synergies comprehend muscle forces ranging from zero to the peak muscle force (Fig. 6) and joint contact force of up to 11.3 BW at the hip (Fig. 7). Up to 60% muscle co-contraction caused a linear increase of muscle and joint forces, whereas higher muscle co-contraction caused a non-linear increase of the same quantities (Fig. 6 and 7). While the probability for these extreme loading conditions to occur has to be determined, these findings may have implications in studying muscle ability to control joint impedance and stability [13], the yet unresolved fracture mechanism for low-energy osteoporotic fractures [46], and may reveal important information for the development of exercise therapies for bone health [47]. Physiologically plausible muscle force patterns well represented the muscle electrical activity input to the model (Fig. 9). Therefore, the proposed approach can be used to study deep aspects of human motion. For example, the calculated spectrum can be used for exploring how different muscles can combine their action in response to the same motor demand.

To the best of the authors' knowledge this is the first numerical study exploring the spectrum of muscle synergies during motion. The model has been shown capable of yielding kinematic, kinetics, hip contact forces and muscle firing patterns in agreement with published patterns for multiple activities [23,25], providing confidence in the reliability of the studied muscle load sharing problem. The large variability of physiologically possible and physiologically plausible muscle forces is consistent with the known ability of the CNS for adopting very different muscle recruitment strategies [16,48]. Although no measurements of the joint contact force under full muscle co-contractions are available, the range of the calculated hip contact force (3.7-11.4 BW) compares well with the hip contact force of 8.7 BW measured by Bergmann and co-workers during stumbling, a value that has been largely attributed to muscle co-contraction rather than to motion dynamics [16]. This provides confidence in the calculated spectrum of muscle forces.

The main limitation of the present study is that the majority of the muscle forces that were not constrained between EMG-driven muscle force boundaries (e.g., the semitendinosus) showed a much higher variability (Fig. 9) than that obtained from repeated EMG recordings, indicating that the calculated spectrum of physiologically plausible muscle forces is larger than that observed in vivo. While it is possible that a reduced number of EMGs input to the model [19] explain the majority of the muscle force variability, the optimal number and type of EMG signals has to be determined. Second, the processed EMG signal was normalised using the peak muscle activation calculated using static optimization, whereas others normalized the processed EMGs to a maximum voluntary contraction task [18,19]. However, a standardized EMG normalization process has yet to be defined [19]. Third, the present results cannot be generalized due to the single anatomy used. More research is necessary to solve this limitation. Fourth, the joint torque was set to the deterministic values calculated using inverse dynamics, thus neglecting the joint torque uncertainties attributable to model assumption and measurement errors [49]. However, this allowed studying the isolated effect of alternative muscle recruitment strategies on calculated muscle and joint forces. Last, the peak isometric muscle stress was the upper boundary of published values (1.37 MPa, [29]), possibly causing an overestimation of calculated forces. However, the upper boundary of muscle forces is a linear function of the peak isometric muscle stress while the lower boundary is almost invariant [23]. Therefore, the boundaries of muscle and joint forces for every intermediate value of the peak isometric stress can be easily extrapolated.

Despite the study limitations, present findings are important for the biomechanics community in that they provide a viable numerical approach for modelling the stochastic nature of the muscle recruitment process. The present results strengthen the notion that muscle co-contraction is important in studying human motion, and provide a viable numerical approach for studying physiological and pathophysiological conditions characterized by complex

sensorimotor behaviours. Moreover, because the proposed approach makes no assumptions on the "normality" of neuromotor control, we expect it to be equally effective in subjects affected by severe neuromuscular pathologies.

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534 **TABLES**

535 Table 1 – The range of the muscle lever arm (cm).

Muscle bundles	The model	Scheys et al., [37]	Arnold et al., [38]	Bonnefoy et al., [39]	White et al. [41]	Kepple et al. [42]	Pierrynowski et al. [43,44]
Hip abduction moment arm							
Gluteus medius anterior	4.7 : 5.7	1.0 : 4.0					
Gluteus medius medial	5.1 : 5.7	1.8 : 4.5					
Gluteus medius posterior	4.1 : 4.9	0.7 : 4.8					
Gluteus minimus anterior	4.1 : 4.7	0.2 : 3.8					
Gluteus minimus medial	4.2 : 5.3	1.0 : 4.0					
Gluteus minimus posterior	4.3 : 5.7	0.0 : 4.2					
Tensor fascia latae	4.7 : 6.8	2.0 : 6.5		6.0 : 7.4	12.4 : 13.2	11.6 : 12.4	3.7 : 5.3
Hip adduction moment arm							
Adductor brevis	5.4 : 7.5	1.0 : 6.0					
Adductor longus	5.3 : 7.0	2.2 : 7.7					
Adductor magnus superior	6.5 : 8.2	3.0 : 6.0					
Adductor magnus medial	6.7 : 7.7	3.0 : 6.0					
Adductor magnus inferior	3.2 : 6.2	2.2 : 6.1					
Gracilis	8.4 : 9.4	1.0 : 7.8		5.6 : 6.2	2.4 : 3.1	2.8 : 4.4	1.5 : 4.5
Hip flexion moment arm							
Ileo-psoas	3.5 : 4.1						
Rectus femoris	2.1 : 4.2	1.9 : 5	2.3 : 3.5	5.3 : 6.1	8.8 : 10.2	9.2 : 11.2	2.4 : 5.0
Sartorius	2.0 : 7.3	1.8 : 7					
Hip extension moment arm							
Biceps femoris long head	2.5 : 6.0	0.2 : 6.0					
Gluteus maximus anterior	4.6 : 5.3	0.0 : 4.0					
Gluteus maximus medial	5.3 : 6.9	0.0 : 4.5					
Gluteus maximus posterior	4.8 : 9.0	0.0 : 6.2					
Semimembranosus	1.4 : 5.4	0.0 : 5.9	3.1 : 4.1				
Semitendinosus	2.2 : 6.3	0.0 : 6.0	3.3 : 5.2				
Knee flexion moment arm							
Biceps femoris long head	4.1 : 5.5			5.7 : 7.1	2.1 : 3.5	3.5 : 4.9	6.1 : 7.1
Biceps femoris short head	3.0 : 4.2						
Semimembranosus	2.9 : 4.1			6.2 : 6.6	2.2 : 5.2	2.7 : 5.3	3.3 : 5.5
Semitendinosus	2.7 : 4.4						
Knee extension moment arm							
Rectus femoris	2.5 : 5.2			3.7 : 4.3	2.1 : 2.7	2.8 : 3.4	4.3 : 5.1
Vastus intermedius	2.6 : 5.3						
Vastus lateralis	2.5 : 5.0						
Vastus medialis	2.4 : 4.9						
Ankle dorsi-flexor moment arm							
Tibialis anterior	3.1 : 3.6			2.5 : 2.9	6.3 : 7.7	3.6 : 4.1	2.3 : 2.5
Extensor digitorum	2.7 : 3.1						
Ankle plantar-flexor moment arm							
Triceps surae	3.4 : 5.0			4.4 : 5.6	4.9 : 6.5	5.3 : 6.5	6.3 : 7.1
Peroneus	1.7 : 2.3			2.8 : 3.0	5.7 : 7.3	2.9 : 4.0	1.7 : 1.9
Tibialis posterior	1.4 : 1.8			2.3 : 2.5	2.9 : 4.3	1.7 : 2.1	1.7 : 1.8
Flexor hallucis	2.1 : 2.2						

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Table 2 – Physiological cross section areas (PCSAs) in the model and corresponding published values (cm^2).

Muscles	Ward et al. [36]^	The donor*	
	Mean (STD)	Left	Right
Psoas major	7.7 (2.3)	3.8	2.9
Iliacus	9.9 (3.4)	4.0	2.7
Gluteus maximus	33.4 (8.8)	27.6	24.1
Gluteus medius	33.8 (14.4)	14.9	15.4
Gluteus minimus	N/A	2.5	N/A
Sartorius	1.9 (0.7)	1.2	1.1
Tensor Fascia Lata	N/A	2.6	2.4
Rectus femoris	13.5 (5.0)	2.1	2.7
Vastus lateralis	35.1 (16.1)	9.3	9.3
Vastus intermedius	16.7 (6.9)	6.4	7.0
Vastus medialis	20.6 (7.2)	11.7	12.0
Gracilis	2.2 (0.8)	1.6	1.3
Adductor longus	6.5 (2.2)	5.1	4.1
Adductor brevis	5 (2.1)	5.4	6.0
Adductor magnus	20.5 (7.8)	12.7	8.5
Biceps femoris long head	11.3 (4.8)	3.3	3.4
Biceps femoris short head	5.1 (1.7)	4.6	4.0
Semitendinosus	4.8 (2.0)	2.9	3.0
Semimembranosus	18.4 (7.5)	12.8	16.1
Tibialis anterior	10.9 (3)	4.3	4.0
Extensor hallucis lonmgus	2.7 (1.5)	1.7	2.7
Extensor digitorum longus	5.6 (1.7)	1.4	3.7
Peroneus longus	10.4 (3.8)	4.5	5.9
Peroneus brevis	4.9 (2.0)	3.4	4.4
Gastrocnemius medial head	21.1 (5.7)	N/A	N/A
Gastrocnemius lateral head	9.7 (3.3)	6.3	6.1
Soleus	51.8 (14.9)	10.5	11.2
Flexor hallucis longus	6.9 (2.7)	N/A	N/A
Flexor digitorum longus	4.4 (2)	2.5	2.6
Tibialis posterior	14.4 (4.9)	1.1	1.4
Mean	13.9 (5.0)	6.1	6.2

* The physiological cross section area was calculated by measuring the muscle volume and length and using published estimates of the pennation angle [50].

^ PCSA values represent the mean and the standard deviation of measurements taken from 21 elderly donors (83 ± 9 years; male:female ratio, 9:12) [36].

FIGURES

Fig. 1: The musculoskeletal model (a), the motion capture scheme (b) and the model during an intermediate frame of walking (c).

Fig. 2: Comparison between the calculated joint torque (solid black) at the hip, the knee and the ankle and the joint torque bands (grey bands) reported by Benedetti et al. [40] for healthy subjects.

Fig. 3: Distance between EMG-driven muscle forces and the solution space of the muscle load sharing problem for an increasing number of EMGs input to the model. In blue, the muscle distance averaged over gait and muscles. In green, the muscle-by-muscle distance averaged over gait.

Fig. 4: Force patterns for the EMG-driven, the static optimization and the best-fit muscle synergy extracted from the solution space of the muscle recruitment problem.

Fig. 5: Linear regression analysis between the EMG-driven muscle forces, the static optimization solution (right) and the best-fit muscle synergy (left).

Fig. 6: Physiologically possible muscle forces. The dashed-black line represents the peak muscle force. The solid-red and solid-blue lines represent the upper and the lower muscle force boundary (low-band passed at 6 Hz, zero-pole design, sixth-order Butterworth filter). Each level represents an admissible muscle co-contraction of 0.2, 0.4, 0.6, 0.8 and 1.

Fig. 7: Physiologically possible hip, knee and ankle contact forces. The shaded grey area represents possible joint forces calculated constraining muscle forces between zero and the peak muscle force. The solid-black lines represent the joint contact force boundary for an admissible muscle co-contraction of 0.2, 0.4, 0.6, 0.8 and 1 (low-band passed at 6 Hz, zero-pole design, sixth-order Butterworth filter).

574 **Fig. 8:** The 15-channel EMG signals for the seven gait trials. The shaded areas represent the
575 0.68 quantile (i.e. mean ± SD) of the EMG distribution. The EMGs sub-set used to
576 calculate the spectrum of physiologically plausible muscle forces is shaded in red.

577 **Fig. 9:** Physiologically plausible muscle forces. The selected muscle force spectrums
578 constrained between EMG-driven force boundaries are shaded in red whereas the
579 remaining muscle force spectrums are shaded in grey. For these latter, the dashed-
580 black line represents the peak muscle force.

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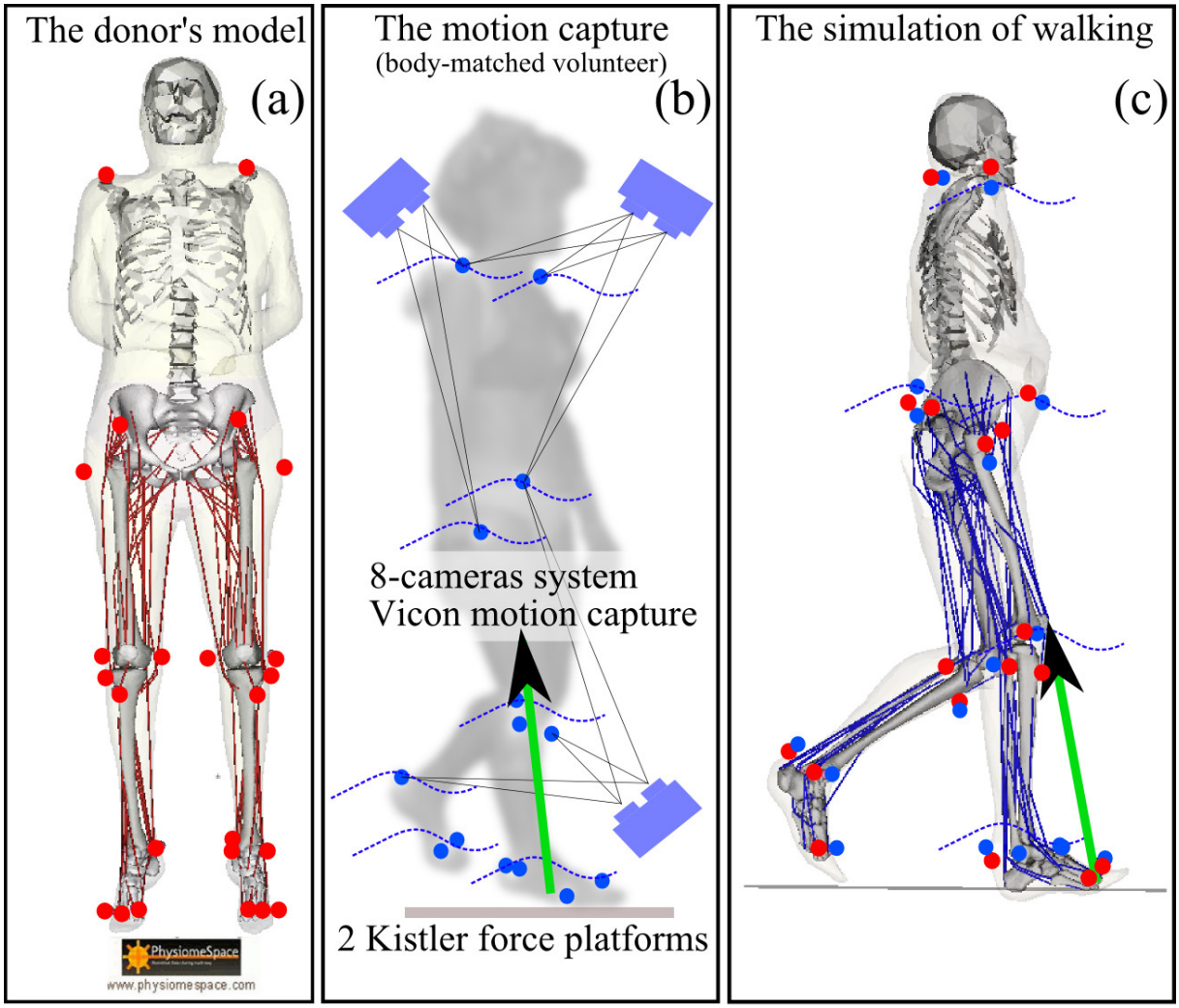
582 **Figure 1**



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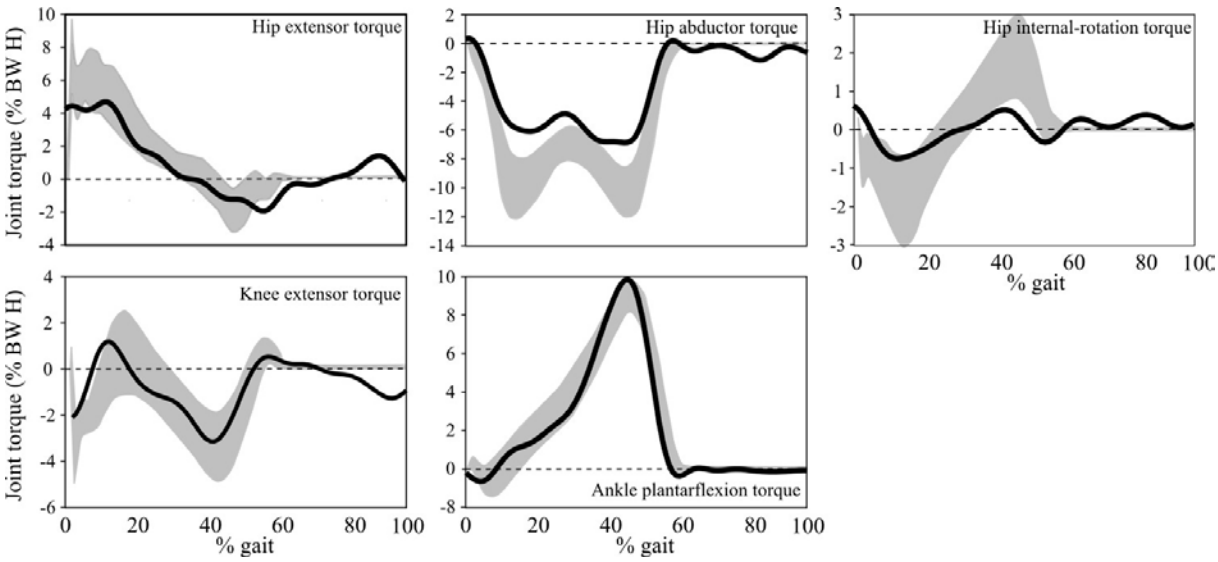
585 Figure2



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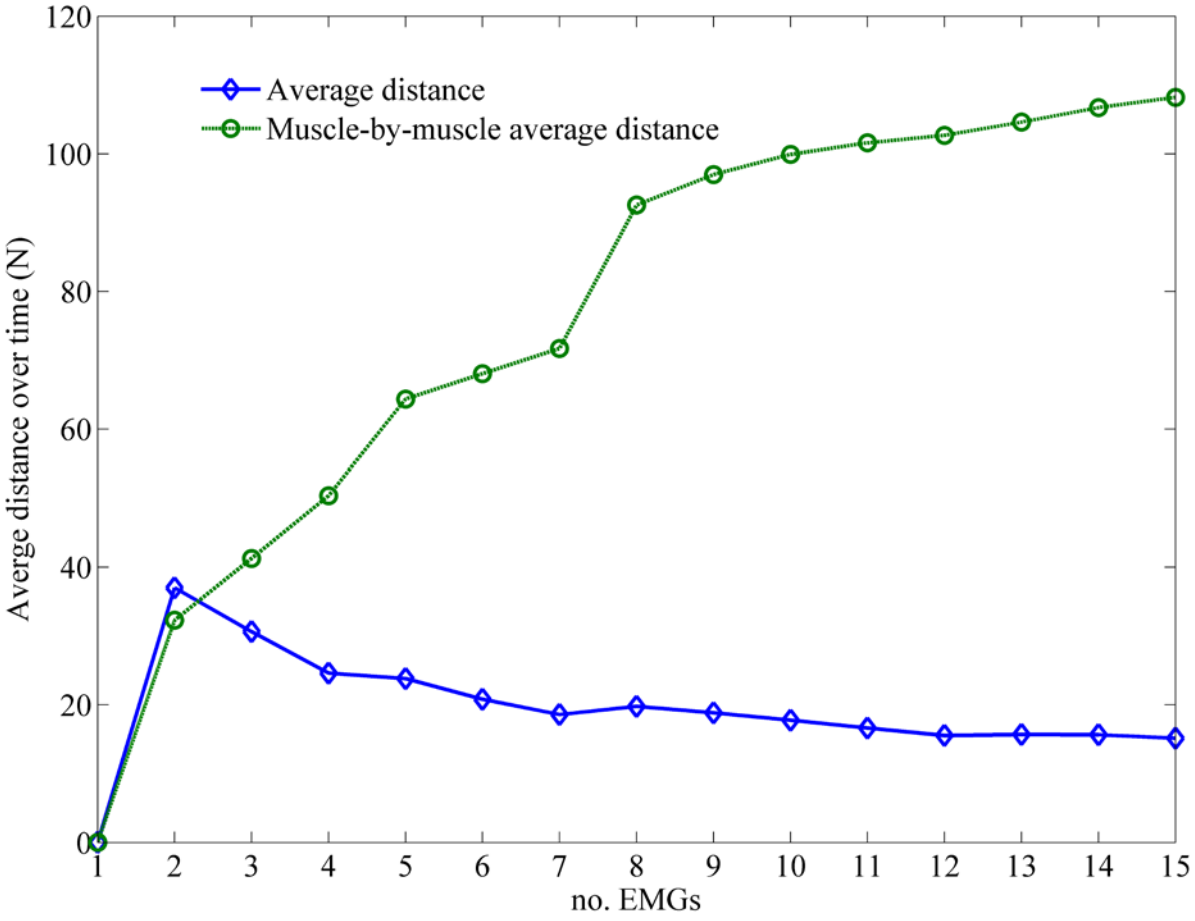
588 Figure 3



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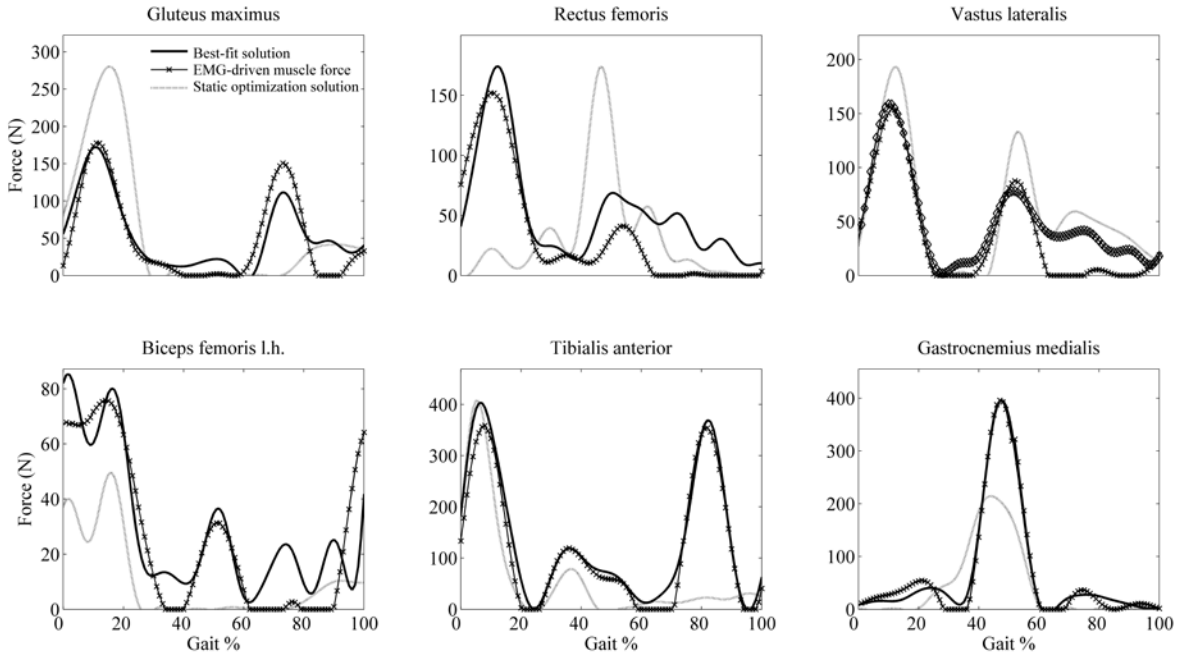
591 Figure 4



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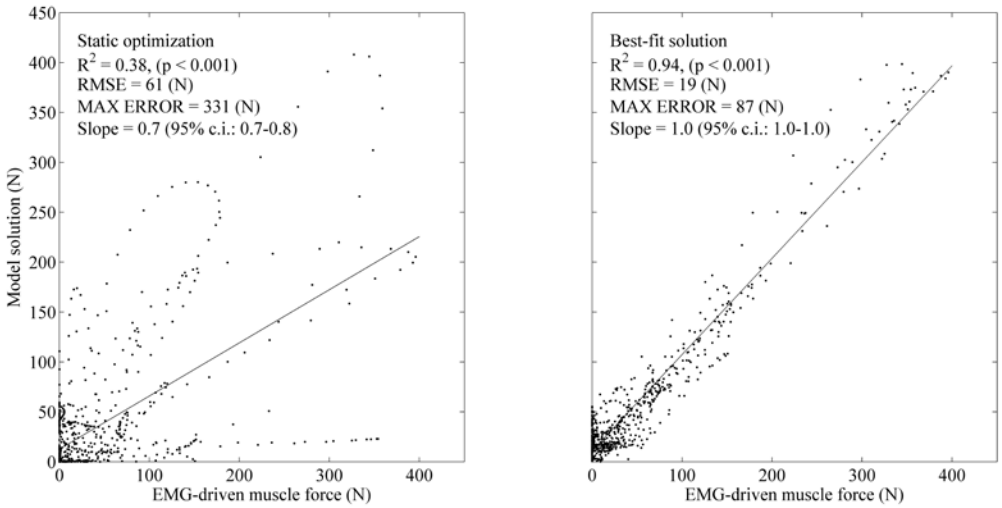
594 Figure 4



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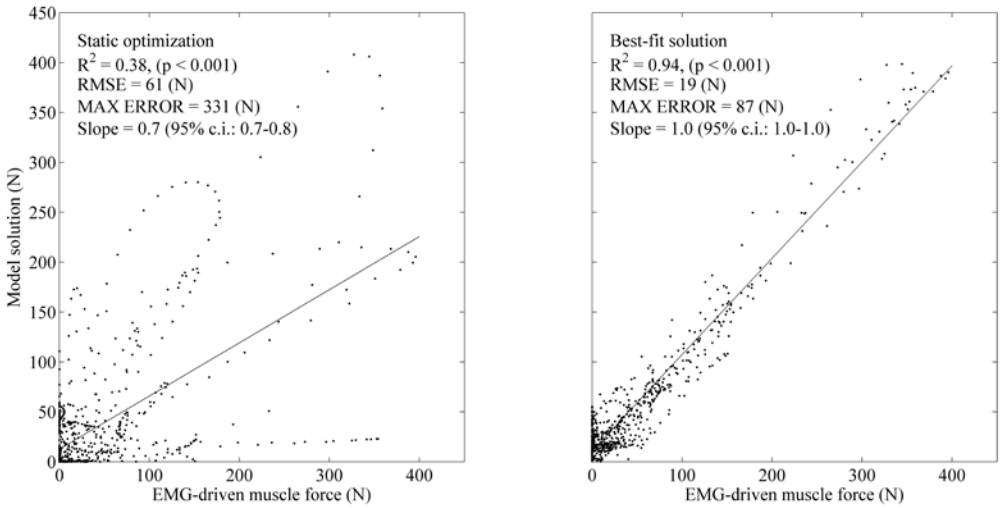
597 Figure 5



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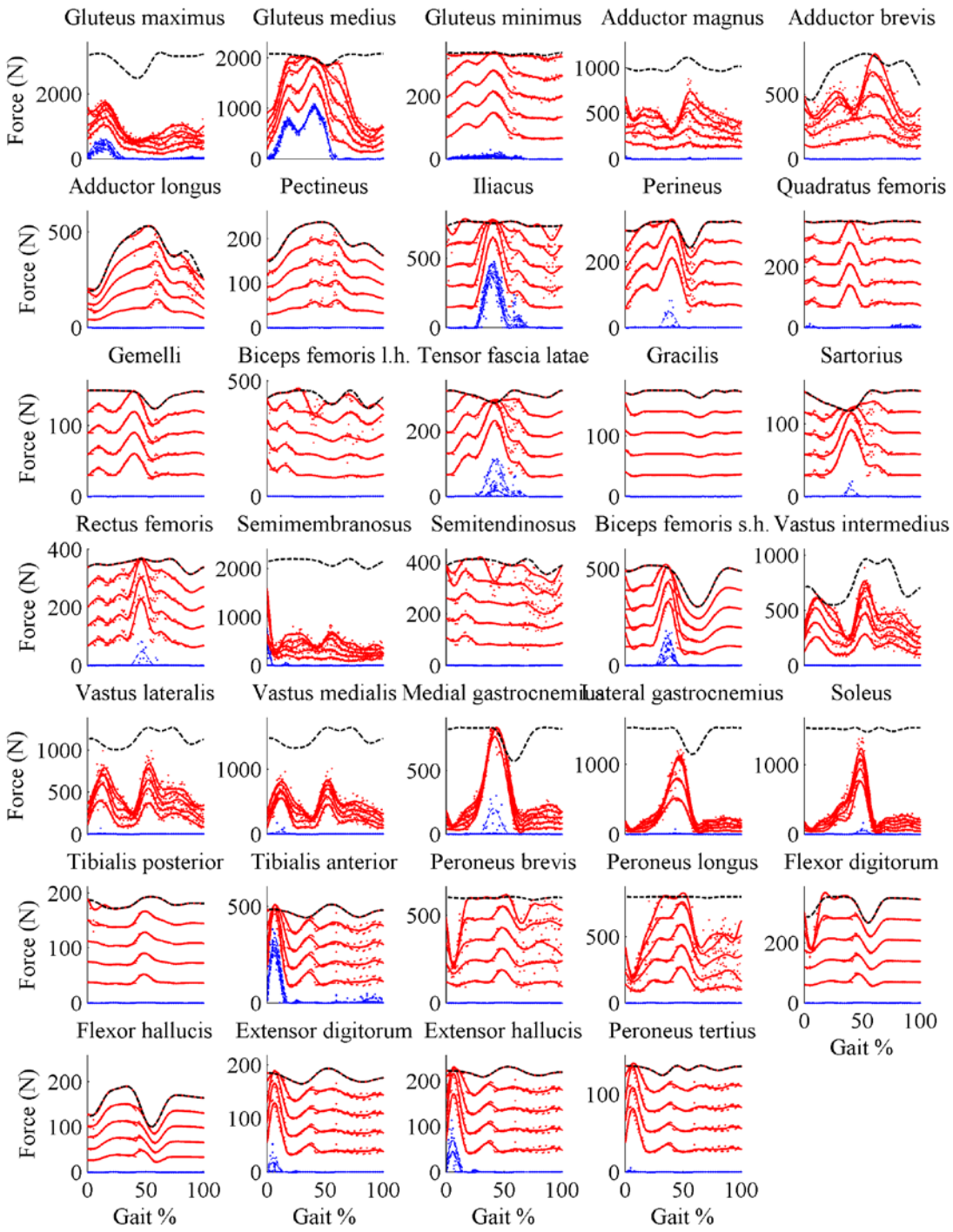
600 Figure 6



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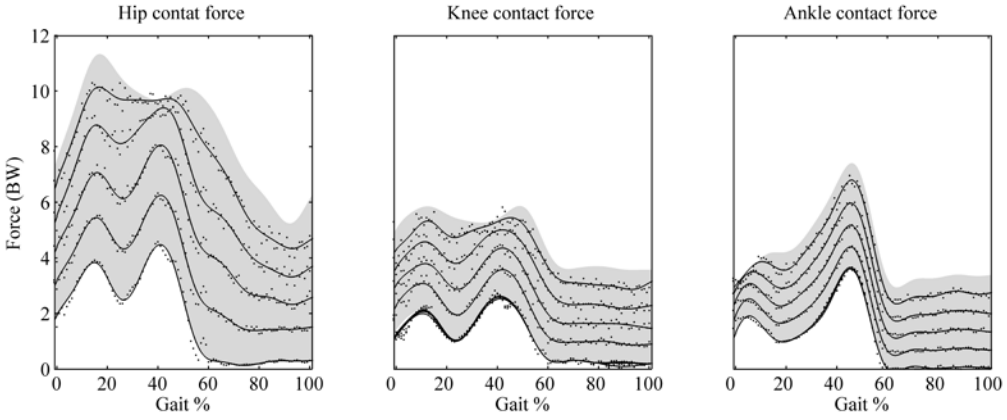
603 Figure 7



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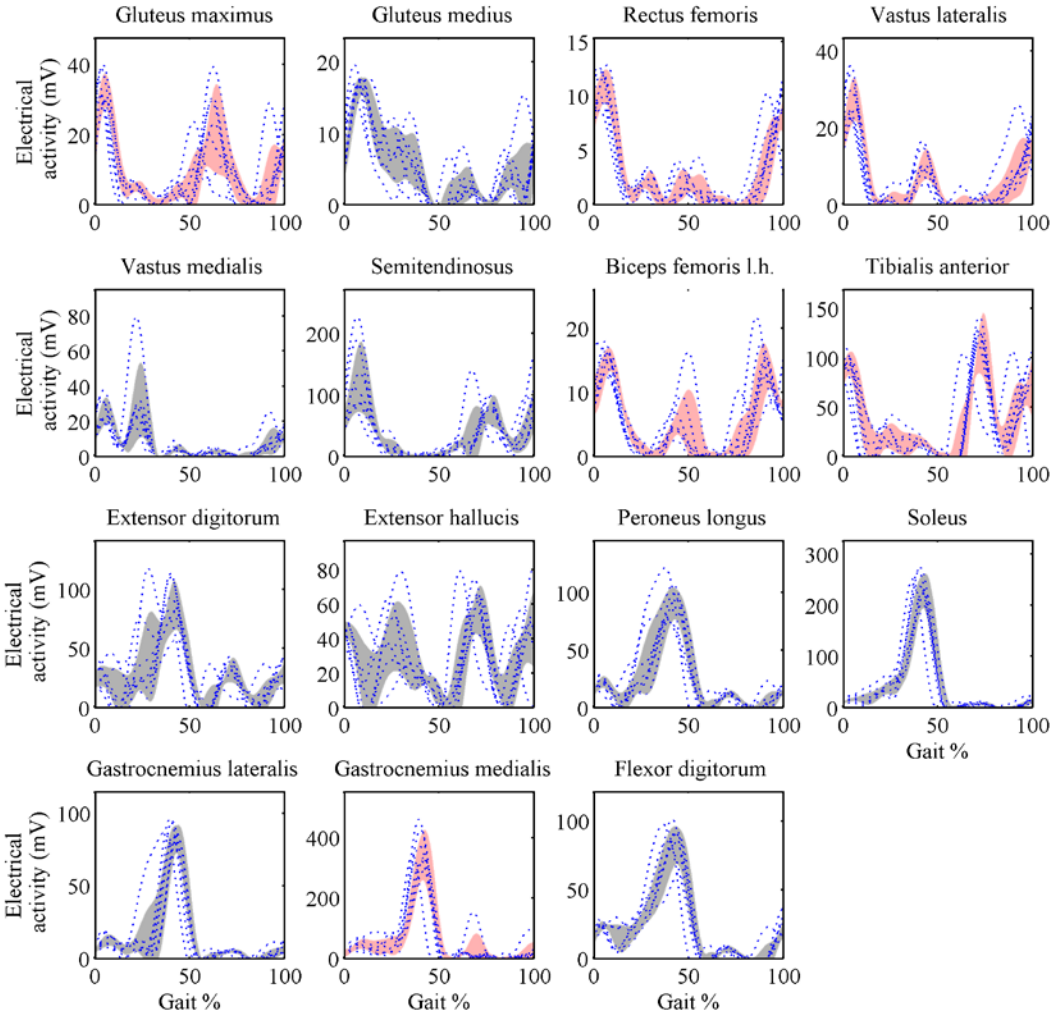
606 Figure 8



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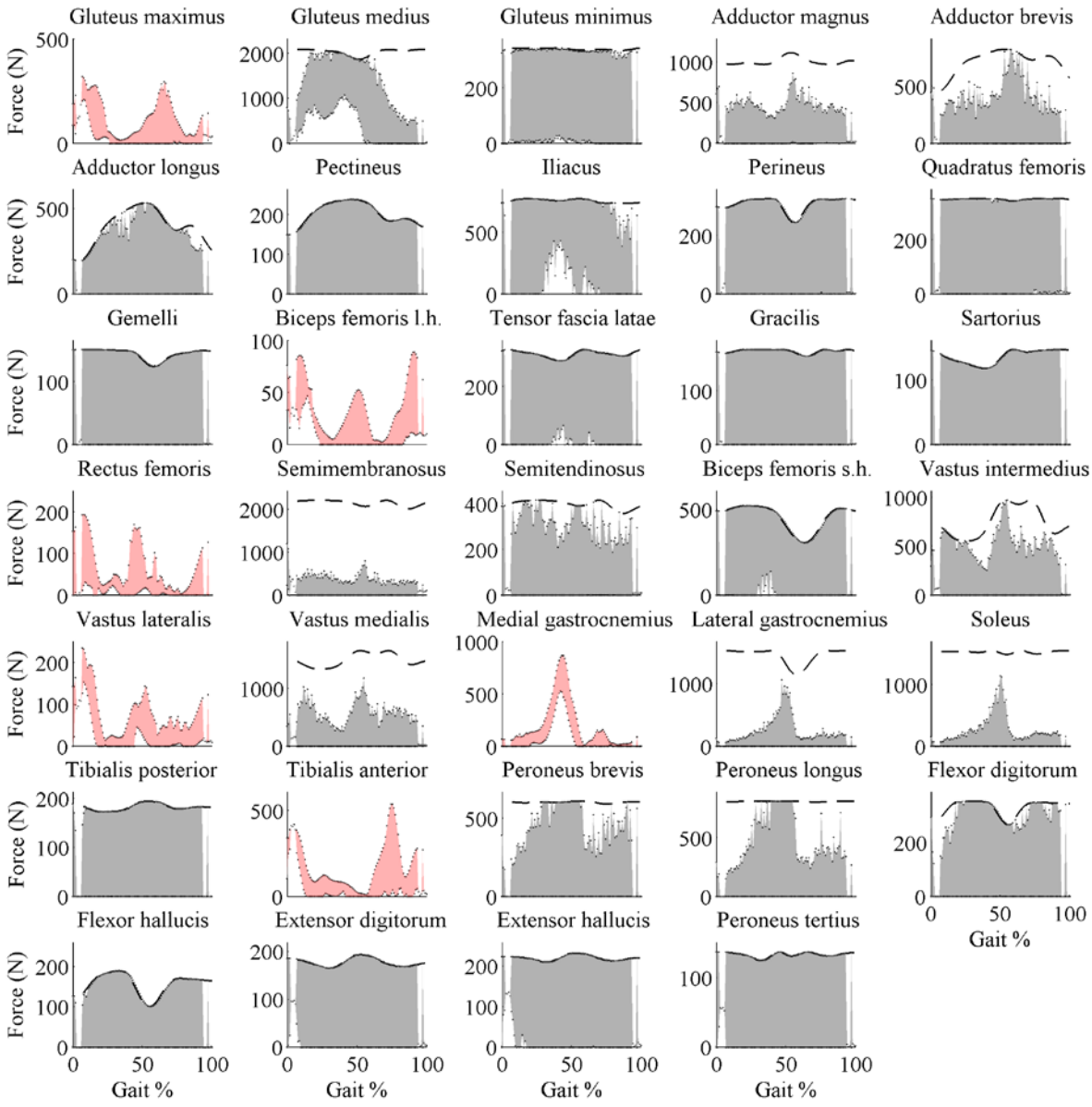
609 Figure 9



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